Studies on Salt Hydrate for Latent Heat Storage. I. Crystal Nucleation of Sodium Acetate Trihydrate Catalyzed by Tetrasodium Pyrophosphate Decahydrate

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The effect of tetrasodium pyrophosphate decahydrate $(Na_4P_2O_7\cdot 10H_2O)$ as a nucleation catalyst for sodium acetate trihydrate $(CH_3CO_2Na\cdot 3H_2O)$ is shown. The supercooled melt of $10\,\mathrm{g}$ of $CH_3CO_2Na\cdot 3H_2O$ recrystallized at about 5 degrees below the melting point only when $0.1\,\mathrm{g}$ of $Na_4P_2O_7\cdot 10H_2O$ was added to it. More than a thousand cycles of alternate heating and cooling through the melting point were carried out in this work. Some observations on nucleation are given and the results are discussed on the basis of crystallographic data.

Sodium acetate trihydrate (CH₃CO₂Na·3H₂O) has received attention recently because of its large latent heat of fusion (about 264 J/g) which makes it attractive as a latent heat storage material.1) But once this material melts, it tends to supercool even if it is cooled considerably below the melting point (58.4 °C).2) One approach to this problem is to add a suitable nucleation catalyst to supercooled CH₃CO₂Na·3H₂O melt. This nucleation catalyst needs to be hardly soluble in CH₃CO₂Na·3H₂O melt so as to not lower the melting point nor diminish the heat of fusion.3) However, such a nucleation catalyst has not been found yet.4,5) In this study, tetrasodium pyrophosphate decahydrate (Na₄P₂O₇·10H₂O) was found to act as a nucleation catalyst for CH₃CO₂Na·3H₂O which hardly lowers the melting point at all and does not diminish the heat of fusion.

We present the results of two different kinds of thermal analysis of $CH_3CO_2Na\cdot 3H_2O$ in the presence of $Na_4P_2O_7\cdot 10H_2O$. One is a heating and cooling cycle of about 30 g samples in a sealed glass vessel, and the other is differential scanning calorimetry of about 15 mg samples. The reason why it acts as a nucleation catalyst for $CH_3CO_2Na\cdot 3H_2O$ is discussed crystallographically and compared to the well known case of borax $(Na_2B_4O_7\cdot 10H_2O)$ for Glawber's Salt $(Na_2SO_4\cdot 10H_2O)$.^{3,6)}

Experimental

Materials. CH₃CO₂Na·3H₂O, Na₄P₂O₇·10H₂O, and Na₂H₂P₂O₇ were obtained commercially and Na₄P₂O₇ was obtained by heating Na₄P₂O₇·10H₂O in an oven at 150—200 °C for 5 h. Na₄P₂O₇·10H₂O was used for experiments after it was ground to a powder and passed through a 100 mesh seive.

Heating and Cooling Cycles of About 30 g Samples in a Sealed Glass Vessel. Weighed quantities of CH₃CO₂Na·3H₂O and Na₄P₂O₇·10H₂O were placed in a glass vessel and the sample was covered with liquid paraffin to prevent water evaporation. The temperature of the sample was measured with a thermocouple, whose junction was placed near Na₄-P₂O₇·10H₂O precipitates because it was expected that recrystallization of CH₃CO₂Na·3H₂O would start on the surface of Na₄P₂O₇·10H₂O crystals. The glass vessel was sealed and put into a water bath. The sample was consecutively heated and cooled at the rate of 0.4 °C/min between 35 °C and 70 °C, and maintained for 30 min each at 35 °C and then 70 °C. In this manner, the melting point t_m and the

temperature at which supercooling was broken t_i were measured and supercooling $\Delta t_i (=t_{\rm m}-t_i)$ was determined in each cycle.

Differential scanning Differential Scanning Calorimetry. calorimetry (DSC) was performed using SSC 560S DSC (Dainiseikosha Co. Ltd.). Weighed quantities of samples were placed in a 15 µl silver crucible and the surface of the sample was covered with one drop of liquid paraffin to prevent water evaporation. The sample was subjected to linearly programmed consecutive heating and cooling in a manner similar to the above. Melting points $t_{\rm m}$ "s were obtained from the sample temperature curve at times corresponding to endothermal peaks and the temperatures at which supercooling was broken t_i "s were obtained from the sample temperature curves at times corresponding to the onset of exothermal peaks. From these temperatures, supercooling $\Delta t_{\rm i}{}'(=t_{\rm m}{}'-t_{\rm i}{}')$ was calculated. This DSC system was calibrated using ice (t_m: 0.0 °C), sodium sulfate decahydrate ($t_{\rm m}$: 32.4 °C) and sodium acetate trihydrate ($t_{\rm m}$: 58.4 °C) as a standard.

Results

The heating and cooling curve for a sample consisting of 30 g of $\mathrm{CH_3CO_2Na\cdot 3H_2O}$ and 0.3 g of $\mathrm{Na_4-P_2O_7\cdot 10H_2O}$ is shown is Fig. 1. The curve shows that the melting point of this sample is 58.4 °C which is the same as that of $\mathrm{CH_3CO_2Na\cdot 3H_2O}$ alone. The supercooling of the sample is broken at 53.1 °C and suddenly the temperature of the sample rises to freezing point, 58.4 °C. After this temperature is maintained for about 12 min, the temperature of sample drops.

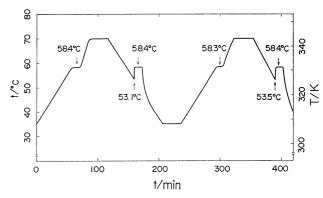


Fig. 1. Heating and cooling curve for a sample consisting of 30 g of CH₃CO₂Na·3H₂O and 0.3 g of Na₄P₂O₇·10H₂O.

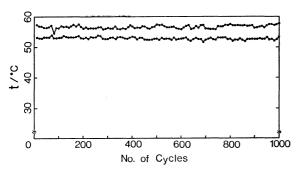


Fig. 2. Changes in melting point t_m and the temperature at which supercooling is broken t_i with cycling.

 \bullet : $t_{\rm m}$, \bigcirc : $t_{\rm i}$.

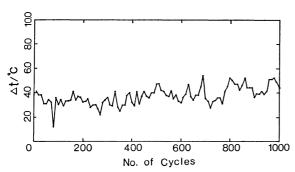


Fig. 3. Changes in supercooling Δt_i with cycling.

In this case, supercooling Δt_i is 5.3 °C.

The melting points $t_{\rm m}$'s and the temperatures at which supercooling is broken $t_{\rm i}$'s are plotted in Fig. 2, with temperature as ordinate and number of cycles as abscissa. As shown in Fig. 2, $t_{\rm i}$ and $t_{\rm m}$ are almost constantly 53 °C and 58.4 °C respectively. The slight scatter of $t_{\rm m}$ falls within measuring error. The supercooling $\Delta t_{\rm i}$ points are plotted in Fig. 3, using the result of Fig. 2. These $\Delta t_{\rm i}$'s are below 6 °C over all the cycles. It was also found that Na₄P₂O₇·10H₂O works continuously as a nucleation catalyst for 1000 cycles. On the other hand, when Na₄P₂O₇·10H₂O powder was not added to CH₃CO₂Na·3H₂O melt, supercooling was not broken down to about 35 °C. These experimental results show that Na₄P₂O₇·10H₂O serves as a very effective nucleation catalyst for CH₃-CO₂Na·3H₂O whose melting point is scarcely lowered.

A DSC curve of a sample consisting of 14.0 mg of CH₃CO₂Na·3H₂O and 1.7 mg of Na₄P₂O₇·10H₂O is illustrated in Fig. 4. The difference between the temperature of the first endothermal peak and that of the second is probably caused by measuring error. The melting points t_m "s and the temperatures at which supercooling is broken t_i "s which are determined by 50 continuous heating and cooling cycles are shown in Fig. 5. The supercooling in this case Δt_i s $(=t_m'$ t_i') are calculated by using the results of Fig. 5 and are plotted in Fig. 6. From Fig. 5, it is found that ti' varies very widely and irregularly with number of cycles and their average is about 45 °C. Thus Δt_i also varies very widely and their average is 13 °C. It is evident that Δt_i is much larger than Δt_i . Moreover, the heat of fusion per 1 g of CH₃CO₂Na·3H₂O which was obtained by this DSC measurement is 262

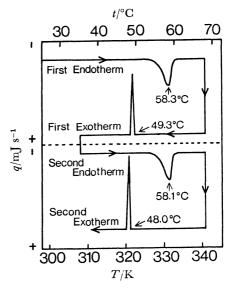


Fig. 4. DSC curve of a sample consisting of 14.0 mg of CH₃CO₂Na·3H₂O and 1.7 mg of Na₄P₂O₇·10H₂O.

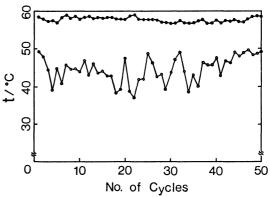


Fig. 5. Changes in melting point $t_{\rm m}$ ' and the temperature at which undercooling is broken $t_{\rm i}$ ' with cycling.

 \bullet : $t_{\rm m}'$, \circ : $t_{\rm i}'$.

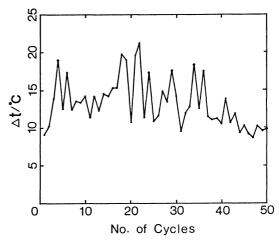


Fig. 6. Changes in undercooling Δt_i with cycling.

J/g, which is good agreement with that of CH₃CO₂Na·3H₂O alone within measuring error. It is understandable that addition of Na₄P₂O₇·10H₂O to CH₃CO₂Na·3H₂O scarcely decreases its heat of fusion.

The solubilities of Na₄P₂O ·10H₂O in CH₃CO₂Na·

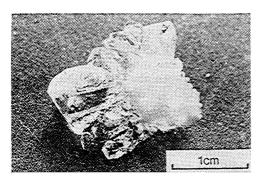


Fig. 7. Photograph of CH₃CO₂Na·3H₂O crystals grown around a mass of Na₄P₂O₇·10H₂O polycrystal.

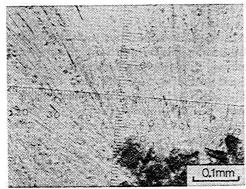


Fig. 8. Micro-photograph of CH₃CO₂Na·3H₂O grown around Na₄P₂O₇·10H₂O particles.

3H₂O melt at 60 °C and 75 °C were both about 0.1 percent by weight. Because of its slight solubility, it is supposed that both the melting point and the heat of fusion of CH₃CO₂Na·3H₂O are hardly influenced by adding Na₄P₂O₇·10H₂O. This is in good agreement with the results obtained by these thermal analyses.

Figure 7 shows CH₃CO₂Na·3H₂O crystals grown around a mass of Na₄P₂O₇·10H₂O polycrystal. The white part indicates a mass of Na₄P₂O₇·10H₂O and transparent crystals around it are CH₃CO₂Na·3H₂O. Figure 8 is a micro-photograph of CH₃CO₂Na·3H₂O crystals grown around Na₄P₂O₇·10H₂O particles. It is observed that CH₃CO₂Na·3H₂O needles are radially grown from Na₄P₂O₇·10H₂O particles. It is suggested that CH₃CO₂Na·3H₂O crystallized as needle since it began to recrystallize at a temperature significantly below the melting point. This large supercooling, we suppose, results from the small sample quantities of this experiment. This is consistent with the result obtained by DSC of about 15 mg sample.

Discussion

Table 1 shows the crystallographic data of $Na_2B_4O_7 \cdot 10H_2O$ and that of $Na_2SO_4 \cdot 10H_2O_7 \cdot 10H_2O_7 \cdot 10H_2O_8 \cdot 10H_2O_7 \cdot 10H_2O_8 \cdot 10H_2O_8$

Table 1. Crystallographic data for sodium sulfate decahydrate and sodium tetraborate decahydrate

| | Na ₂ SC | $0_4 \cdot 10 H_2 O$ | $Na_2B_4O_7 \cdot 10H_2O$ |
|---------------------|--------------------|----------------------|---------------------------|
| Crystal system | Monoclinic | | Monoclinic |
| Space group | $P2_1/c$ | | C2/c |
| Unit-cell parameter | $a/\mathrm{\AA}$ | 11.512 | 11.885 |
| | $b/{ m \AA}$ | 10.370 | 10.654 |
| | $c/\mathrm{\AA}$ | 12.847 | 12.206 |
| | <i>β</i> /° | 107.789 | 106.623 |
| | $V/{ m \AA}^3$ | 1460 | 1481 |
| | \boldsymbol{Z} | 4 | 4 |

Table 2. Crystallographic data for sodium acetate trihydrate and tetrasodium pyrophosphate decahydrate

| (| $\mathrm{CH_3CO_2Na\cdot 3H_2O}$ | | $Na_4P_2O_7 \cdot 10H_2O$ |
|---------------------|----------------------------------|--------|---------------------------|
| Crystal system | Monoclinic | | Monoclinic |
| Space group | C2/c | | C2/c |
| Unit-cell parameter | $a/\mathrm{\AA}$ | 12.353 | 17.01 ± 0.02 |
| | $b/\mathrm{\AA}$ | 10.466 | 6.96 ± 0.01 |
| | $c/\mathrm{\AA}$ | 10.401 | 14.85 ± 0.02 |
| | β/° | 111.69 | 112.0 ± 0.2 |
| | $V/{ m \AA}^3$ | 1249.5 | 1630 |
| | Z | 8 | 4 |

lographic similarities have been pointed out to be the cause of the nucleation catalysis.⁷⁾

On the other hand, both $Na_4P_2O_7 \cdot 10H_2O$ and CH_3 -CO₂Na·3H₂O are monoclinic and have the same space group C2/c, however their lattice constants a, b, and c are greatly different. In the crystal structure of CH₃CO₂Na·3H₂O, Na ion has distorted octahedral coordination with six oxygen atoms which consist of one acetate oxygen and five water molecules. Adjacent octahedra share an edge and form a continuous chain along the z axis.9,10) However, the crystal structure of Na₄P₂O₇·10H₂O contains two types of sodium atoms lying within octahedra, which are made up of six water molecules in the one case, and four water molecules and two oxygen atoms of a pyrophosphate group in the other case. The Na(H₂O)₆ octahedra share edges and corners with each other so as to build up sheets of linked octahedra. The other octahedron containing a pyrophosphate group shares two edges with the $Na(H_2O)_6$ octahedra so as to link to the sheets of $Na(H_2O)_6$ octahedra.^{8,11)} Thus it is deduced that the structures of CH₃CO₂Na·3H₂O and Na₄P₂O₇· 10H₂O do not have highly similar chains or sheets of water molecules-coordinate Na ions, whereas Na₂-SO₄·10H₂O and Na₂B₄O₇·10H₂O have remarkably similar chains.

The lattice spacings on low index planes of CH₃-CO₂Na·3H₂O and Na₄P₂O₇·10H₂O which can be calculated from the lattice constants shown in Table 2 are listed in Table 3. In this table, the lattice spacings on planes of Na₄P₂O₇·10H₂O which agree with those of CH₃CO₂Na·3H₂O within 1%, are written in the same row of those of CH₃CO₂Na·3H₂O. It can be seen that there are many planes of CH₃CO₂Na·3H₂O whose lattice spacing is close to that of Na₄P₂O₇·10H₂O.

Table 3. Lattice spacing on low index planes of sodium acetate trihydrate and that of tetrasodium pyrophosphate decahydrate

| $\mathrm{CH_3CO_2Na\cdot 3H_2O}$ | | $Na_4P_2O_7 \cdot 10H_2O$ | | |
|----------------------------------|-------|---------------------------|--------------------|--|
| (hkl) | d/Å | $d/	ext{\AA}$ | (hkl) | |
| ` , | • | 15.77 | (100) | |
| | | 13.77 | (001) | |
| | | 13.08 | $(10\overline{1})$ | |
| (100) | 11.48 | | | |
| (010) | 10.47 | | | |
| (001) | 9.665 | | | |
| $(10\overline{1})$ | 9.272 | | | |
| | | 8.858 | (101) | |
| | | 8.317 | $(20\overline{1})$ | |
| | | 7.886 | (200) | |
| (110) | 7.734 | | | |
| | | 7.409 | $(10\overline{2})$ | |
| (011) | 7.100 | | | |
| $(11\overline{1})$ | 6.940 | 6.960 | (010) | |
| | | 6.834 | (002) | |
| | | 6.540 | $(20\overline{2})$ | |
| (101) | 6.330 | 6.368 | (110) | |
| | | 6.211 | (011) | |
| | | 6.144 | $(11\overline{1})$ | |
| $(20\overline{1})$ | 6.004 | 5.949 | (201) | |
| (200) | 5.739 | | _ | |
| | | 5.670 | $(30\overline{1})$ | |
| | | 5.588 | (102) | |
| | | 5.473 | (111) | |
| (111) | 5.416 | | _ | |
| | | 5.338 | $(21\overline{1})$ | |
| (020) | 5.233 | 5.257 | (300) | |
| $(21\overline{1})$ | 5.208 | 5.228 | $(30\overline{2})$ | |
| $(10\overline{2})$ | 5.193 | 5.218 | (210) | |
| (210) | 5.032 | 5.073 | $(11\overline{2})$ | |

For example, $d(11\bar{1})$ of $CH_3CO_2Na\cdot 3H_2O$ agrees very closely with d(010) of $Na_4P_2O_7\cdot 10H_2O$. Consequently, the reason why $Na_4P_2O_7\cdot 10H_2O$ serves as an effective nucleation catalyst for $CH_3CO_2Na\cdot 3H_2O$ is considered to be their close resemblance in lattice spacing on certain low index planes.

The extent of supercooling of $Na_2SO_4\cdot 10H_2O$ containing $Na_2B_4O_7\cdot 10H_2O$ is known to be 1-2 °C in the experiment using test tube³) and 7 °C in DSC.¹²) On the other hand, the extent of supercooling of $CH_3-CO_2Na\cdot 3H_2O$ containing $Na_4P_2O_7\cdot 10H_2O$ is found to be about 5 °C in the experiment using sealed glass vessel and at an average of 13 °C in DSC. In each case, the extent of supercooling of $CH_3CO_2Na\cdot 3H_2O$ containing $Na_4P_2O_7\cdot 10H_2O$ is larger than that of $Na_2SO_4\cdot 10H_2O$ containing $Na_2B_4O_7\cdot 10H_2O$. As indicated before, $Na_2SO_4\cdot 10H_2O$ and $Na_2B_4O_7\cdot 10H_2O$ have analogous unit cells and remarkably similar chains

which are formed by sharing two edges of $Na(H_2O)_6$ octahedra each other, whereas $CH_3CO_2Na\cdot 3H_2O$ and $Na_4P_2O_7\cdot 10H_2O$ only resemble each other in lattice spacing on certain low index planes. The difference of supercooling between the $CH_3CO_2Na\cdot 3H_2O$ system and $Na_2SO_4\cdot 10H_2O$ system is considered to be due to such a different modes of resemblance in crystal structure.

It was pointed out that there was difference between the supercooling of $\rm Na_2SO_4\cdot 10H_2O$ containing $\rm Na_2B_4O_7\cdot 10H_2O$ obtained by the heating and cooling cycles using sealed test tube and that obtained by using DSC.¹³) The cause of this difference of supercooling extent for the $\rm CH_3CO_2Na\cdot 3H_2O$ system is not more clearly understood than for the $\rm Na_2SO_4\cdot 10H_2O$ system.

In addition, both anhydrous sodium pyrophosphate $(Na_4P_2O_7)$ and sodium hydrogenpyrophosphates such as disodium dihydrogenpyrophosphate $(Na_2H_2P_2O_7)$ were found to act as a nucleation catalyst as well as $Na_4P_2O_7\cdot 10H_2O$. This effect comes from the fact that a part of $Na_4P_2O_7$ and $Na_2H_2P_2O_7$ become $Na_4P_2O_7\cdot 10H_2O$ in $CH_3CO_2Na\cdot 3H_2O$ melt. The presence of $Na_4P_2O_7\cdot 10H_2O$ both in the mixture of 30 g of $CH_3CO_2Na\cdot 3H_2O$ melt and 1 g $Na_4P_2O_7$ and in the mixture of 30 g of $CH_3CO_2Na\cdot 3H_2O$ melt and 1 g of $Na_2H_2P_2O_7$ was confirmed by X-ray diffraction.

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